

WHAT IS CLAIMED IS:

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1. A method for reducing a precision of an input datum having a precision portion and a loss portion, comprising:
- a. comparing the loss portion to a preselected threshold value, f_t ;
 - b. determining a selectable bias, α , responsive to the loss portion being in a defined relation to the preselected threshold value, f_t ; and
 - c. combining the precision portion with α , creating a reduced precision datum thereby,
wherein α corresponds to a predetermined characteristic of one of α , the input datum, the reduced precision datum, and a combination thereof.
2. The method of claim 1, wherein determining the selectable bias further comprises one of:
- a. assigning a first value to α , responsive to the loss portion being substantially equal to f_t ;
 - b. assigning a second value to α , responsive to the loss portion being less than f_t ; and
 - c. assigning a third value to α , responsive to the loss portion being greater than f_t .
3. The method of claim 1, further comprising determining the selectable bias responsive to a predetermined characteristic

of a plurality of input data relative to a corresponding
plurality of reduced precision data.

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4. The method of claim 1, further comprising determining the
selectable bias responsive to a predetermined characteristic
attributable to reducing the precision of the input datum.

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5. The method of claim 1, further comprising determining the
selectable bias responsive to the predetermined
characteristic of the selectable bias, the predetermined
characteristic being the mean value of a plurality of
selectable bias values.

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6. The method of claim 2, further comprising determining the
selectable bias responsive to a predetermined characteristic
of a plurality of input data relative to a corresponding
plurality of reduced precision data, and the predetermined
characteristic being attributable to reducing the precision.

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7. The method of claim 6, wherein the predetermined
characteristic is a predetermined mean error value.

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8. The method of claim 2, further comprising determining the
selectable bias responsive to a predetermined characteristic

of one of input data, a corresponding reduced precision
data, and a combination thereof.

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9. The method of claim 8, wherein the predetermined
characteristic comprises a predetermined statistical value.

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10. The method of claim 4, wherein the predetermined
characteristic comprises a predetermined mean error value
of the plurality of reduced precision data relative to a
corresponding plurality of input data.

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11. The method of claim 9, wherein the predetermined statistical
value comprises the mean value of the reduced precision data
relative to a corresponding plurality of finite-precision
fixed point input data.

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12. The method of claim 2, further comprising assigning a fourth
value to α , responsive to α being substantially equal to f_t ,
the fourth value being in a predefined relationship with the
first value.

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13. The method of claim 12, further comprising determining the
selectable bias responsive to a predetermined characteristic
of input data relative to corresponding reduced precision

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5 data, and the predetermined characteristic being a preselected mean error value associated therewith.

10 14. The method of claim 12, wherein:

- 15 a. the f_t is approximately equal to 0.5_{10} ;
- b. the first value is 1 when the value of the loss portion substantially equals about 0.5_{10} , the input datum is a negative-valued datum, with the first value being added to the precision portion;
- c. the second value is zero when value of the loss portion is less than about 0.5_{10} ;
- d. the third value is 1 when the value of the loss portion is greater than about 0.5_{10} , with the third value being added to the precision portion;
- e. the fourth value is 0 when the loss portion substantially equals about 0.5_{10} , and the input datum is a positive-valued datum; and
- 20 f. the preselected mean error value relative to the input datum and the reduced precision datum is minimized.

25 15. The method of claim 11, wherein:

- 30 a. f_t is substantially equal to 0.5_{10} ;
- b. the first value is a current first value being selected to be one of '1' and '0' when the value of

the loss portion substantially equals about 0.5_{10} , in a predefined relationship to a previous first value;

- c. the second value is zero when the loss portion is less than about 0.5_{10} ; and
 - d. the third value is 1 when the loss portion is greater than about 0.5_{10} , with the third value is added to the value of the precision portion.

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16. The method of claim 14, wherein the predefined relationship is an alternating relationship.

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17. The method of claim 16, wherein the alternating relationship is a toggle relationship with the current first value being zero if the previous first value was 1, and the current first value being 1 if the previous first value was zero, and wherein the preselected mean error value is minimized responsive to the alternating relationship.

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18. The method of claim 15, wherein the alternating relationship includes a selectable number of 1's being interleaved with a selectable number of zeros, the mean value of the reduced precision data being responsive to the alternating relationship.

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19. The method of claim 2, wherein each of the input datum and
5 the reduced precision datum are represented by two's complement fixed point values.

10 20. The method of claim 16, wherein the alternating relationship includes a selected pseudorandom sequence of data bits.

15 21. A method for rounding a first datum, \mathbf{x} , having precision of a digits, to a second datum, $\mathbf{\tilde{x}}$, having precision of b digits, wherein $a > b$, first b digits of \mathbf{x} being a precision portion, and remaining $a-b$ digits of \mathbf{x} being a loss portion, the method comprising:

20 a. evaluating the loss portion relative to a preselected rounding threshold value;

25 b. if the loss portion is substantially equal to the preselected threshold, then defining $\mathbf{\tilde{x}}$ according to the equation:

$$\mathbf{\tilde{x}} = \mathbf{x} + 2^{-(b+1)}\alpha,$$

where α is a selectable bias represented by a rounding digit;

30 c. if the loss portion is not substantially equal to the preselected threshold, then defining $\mathbf{\tilde{x}}$ according to the equation:

$$\mathbf{\tilde{x}} = \mathbf{x} + 2^{-(b+1)}; \text{ and}$$

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d. eliminating the loss portion of \mathbf{x} , producing \mathbf{x}' thereby.

22. The method of claim 21, wherein selectable bias α is representative of a predetermined characteristic of one of \mathbf{x} , \mathbf{x}' , α , and a combination thereof.

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23. The method of claim 22, wherein the preselected threshold is substantially equivalent to 0.5_{10} .

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24. The method of claim 23, wherein the predetermined characteristic comprises a preselected mean error value of \mathbf{x} relative to \mathbf{x}' .

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25. The method of claim 24, wherein the preselected mean error value, $E(\epsilon)$, is substantially defined by the equation:

$$E(\epsilon) = 2^{-a}(E(\alpha) - \beta_2),$$

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where $E(\alpha)$ is a mean value of selectable bias α .

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26. The method of claim 25 wherein the mean value of the selectable bias is substantially within the range of

$$0.0 \leq E(\alpha) < 1.0$$

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27. The method of claim 26, wherein the mean value of the selectable bias, $E(\alpha)$, is approximately equal to

5 preselected mean error value, $E(e)$, and $E(\alpha)$ is
approximately zero.

- 10 28. The method of claim 27, wherein the predetermined characteristic further comprises a preselected error variance value, σ_e^2 , substantially defined by the equation:

$$\sigma_e^2 = \frac{2^{-2b} + 2^{-(2a-1)}}{12}$$

- 15 29. The method of claim 28, wherein the rounding digit is selected from a alternating sequence of digits in the pair of digits <0,1>.

- 20 30. The method of claim 28, wherein the rounding digit is selected from a pseudorandom sequence of binary digits.

- 25 31. A method for rounding a first two's complement fixed point datum, x , having an integer part of n bits, a fractional part of a bits the integer part, and sign bit, s_i , to a second two's complement fixed point datum, \bar{x} , having a fractional part of b bits following the radix point, where a and b are representative of the respective precisions of x and \bar{x} , and where $a > b$, comprising:
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- 5 a.. evaluating the fractional part of X and defining y as
the most significant bit (MSB) of the a bits;
b. if the first bit following the radix point of X is
equal to a 1 bit trailed by $(a-1)$ zero bits, then
defining \hat{X} according to the equation:

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$$\hat{X} = n + s_i$$

15 and

- c. otherwise, defining \hat{X} according to the equation:

$$\hat{X} = n + y$$

20 32. The method of claim 31, wherein the occurrence of positive
numbers and negative numbers in a plurality of the datum,
 X , is substantially equiprobable.

25 33. A method for rounding signal values, comprising:
is desired; and

20 a. detecting a predetermined state value wherein rounding
b. rounding the state value according to one of
30 i. an alternating round-up/round-down method and
ii. a sign addition round-up/round-down method.

35 34. An arithmetic device, comprising a bias generator
producing a selectable bias α , responsive to a predetermined
signal characteristic, the device receiving an input signal and

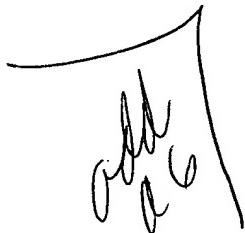
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coupling the selectable bias α thereto.

5 35. The arithmetic device of claim 34, further comprising
a combiner coupled to the bias generator, the combiner receiving
and combining the input signal and the selectable bias α , and
10 producing an output signal.

36. The arithmetic device of claim 34 further comprising
wherein the bias generator further comprises a comparator for
15 comparing the input signal to a preselected threshold value, the
comparator urging the bias generator to produce the selectable
bias α responsive to the preselected threshold value.

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